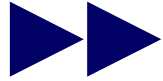


Information Extraction by Grammatical  
Inference  
G. Grieser



# Information Extraction by Grammatical Inference

Gunter Grieser  
FG Intellektik, FB Informatik  
TU Darmstadt

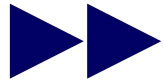
Information Extraction

Wrappers

AEFS

Learning

# Information Extraction by Grammatical Inference G. Grieser



## *Overview*

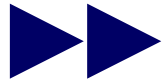
- Information extraction
- wrappers
  - island wrappers
- representation language
  - EFS, AEFS
  - representability
- learning
  - learning models LIM and PAC
  - learning of AEFS, of island wrappers, and of the subtasks

Information Extraction

Wrappers

AEFS

Learning



*Computers: from toolboxes to assistants*

computer as **tool**

does what I **say**

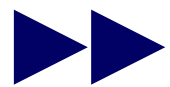
- artificial communication
- machine logic
- no world knowledge,  
no context

computer as **assistant**

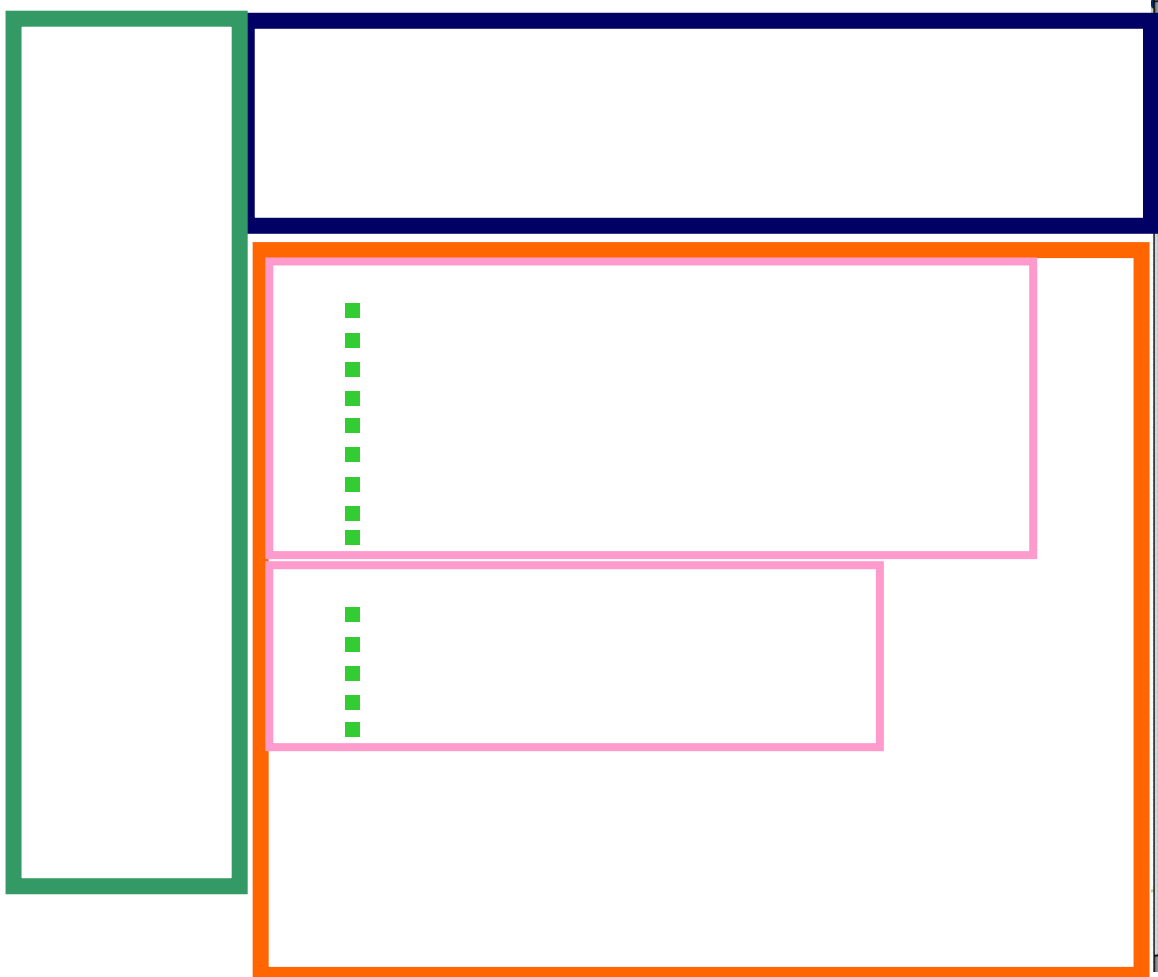
does what I **mean**

- my communication style
- thinking amplifier
- context, world knowledge

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*Consider information in a web page*

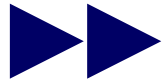


Information Extraction

Wrappers

AEFS

Learning



*Motivation for IE*

## How to extract information from such documents?

there is some growing interest in powerful information extraction procedures, e.g.

to allow for an explicit access to information that is hidden in various documents (knowledge management)

as a result thereof, there is some growing need for techniques that allow for an ,interactive‘ creation of powerful information extraction procedures

### Neue Suche

Produkt/Dienstleistung



### Durchsuchen

- ▶ Über TGR Europe
- ▶ Werben
- ▶ Medienpaket
- ▶ TGR Europe Ansprechpartner
- ▶ Kostenlose TGR Europe CD-ROM
- ▶ TGR Europe kontaktieren
- ▶ Kostenloser Eintrag
- ▶ Firmenpolitik
- ▶ Links
- ▶ Referenzen
- ▶ Trade Shows
- ▶ Internationale Informationen.



Suche >> Kohlenmonoxid

Zu Firmen in:

Belgien

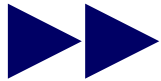
TGR Europe fand **64 Firmen** unter "Kohlenmonoxid"

GO

### Belgien (9)

- [AGA SA](#) (Zemst)
- [Air Products NV/SA](#) (Brussel/Bruxelles)
- [Air Products SA Continental Europe Specialty Gases Facility](#) (Sombrefe)
- [BASF Belgium SA/NV](#) (Brussel/Bruxelles)
- [Hoek Loos NV](#) (Niel)
- [Indugas NV](#) (Schoten)
- [International Gas & Services NV](#) (willebroek)

# Information Extraction by Grammatical Inference G. Grieser



*Documents are available as source code only!*

```
href="http://www.tgreurope.com/main/gotocompany/11307307302347372307350390"  
      fontsize="+1">L' Air Liquide GmbH</A><FONT
```

```
size=1>&nbsp;(D&uuml;sseldorf) &nbsp;&nbsp;</FONT><BR></LI></BLOCKQUOTE></TD></  
TR>
```

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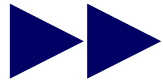
```
href="http://www.tgreurope.com/main/gotocompany/12309309317335386346340304"  
      fontsize="+1">Messer Griesheim GmbH  
Industriegase Krefeld</A><FONT
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      fontsize="+1">Tyczka Industrie-Gase  
GmbH</A><FONT
```

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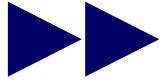


*IE and formal languages*

- documents are strings over a certain alphabet
- information is contained in the documents
- can view documents as well as contained information as formal languages



# Information Extraction by Grammatical Inference G. Grieser



*Oftentimes, information can be identified by its context*

```
href="http://www.tgreurope.com/main/gotocompany/11307307302347372307350390"  
    fontsize="+1">L' Air Liquide GmbH</A><FONT
```

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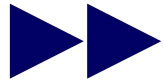
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    fontsize="+1">Tyczka Industrie-Gase  
GmbH</A><FONT
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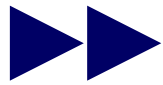
Information Extraction by Grammatical  
Inference  
G. Grieser



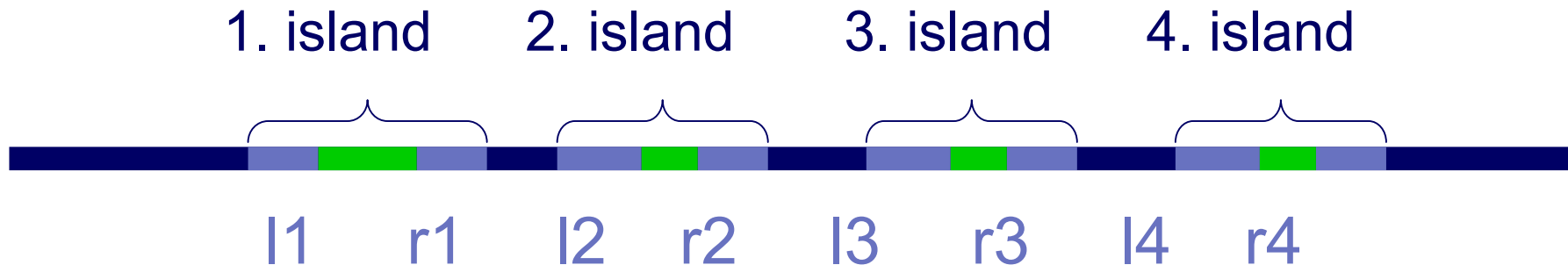
*IE and formal languages*

- documents are strings over a certain alphabet
- information is contained in the documents
- can view documents as well as contained information **as well as context** as formal languages

Information Extraction by Grammatical  
Inference  
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*Island Wrappers*



in general: delimiters not unique

⇒ delimiter languages

n: arity of the island wrapper

⇒  $2n$  delimiter languages:  $L_1, R_1, \dots, L_n, R_n$

**island wrapper**:  $2n$ -tuple of formal languages

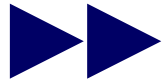
$(L_1, R_1, \dots, L_n, R_n)$

Information Extraction

**Wrappers**

AEFS

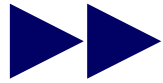
Learning



*Island Wrapper: definition*

an island wrapper  $(L_1, R_1, \dots, L_n, R_n)$  extracts a tuple  $(v_1, v_2, \dots, v_n)$  from document  $d$  iff:

- $d = x_1 l_1 v_1 r_1 x_2 l_2 v_2 r_2 x_3 \dots x_n l_n v_n r_n x_{n+1}$
- $x_1 \in \Sigma^*$   $x_{n+1} \in \Sigma^*$
- $l_1 \in L_1$   $r_1 \in R_1$   $l_2 \in L_2$   $r_2 \in R_2$  ...  $l_n \in L_n$   $r_n \in R_n$
- $v_1 \in \Sigma^+ \setminus (\Sigma^* R_1 \Sigma^*)$  ...  $v_n \in \Sigma^+ \setminus (\Sigma^* R_n \Sigma^*)$

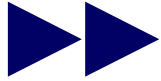


*Island wrapper: definition*

an island wrapper  $(L_1, R_1, \dots, L_n, R_n)$  extracts a tuple  $(v_1, v_2, \dots, v_n)$  from document  $d$  iff:

- $d = x_1 l_1 v_1 r_1 x_2 l_2 v_2 r_2 x_3 \dots x_n l_n v_n r_n x_{n+1}$
- $x_1 \in \Sigma^* \quad x_{n+1} \in \Sigma^*$
- $l_1 \in L_1 \quad r_1 \in R_1 \quad l_2 \in L_2 \quad r_2 \in R_2 \quad \dots \quad l_n \in L_n \quad r_n \in R_n$
- $v_1 \in \Sigma^+ \setminus (\Sigma^* R_1 \Sigma^*) \quad \dots \quad v_n \in \Sigma^+ \setminus (\Sigma^* R_n \Sigma^*)$
- $x_2 \in \Sigma^* \setminus (\Sigma^* L_2 \Sigma^*) \quad \dots \quad x_n \in \Sigma^* \setminus (\Sigma^* L_n \Sigma^*)$

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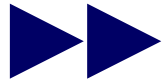
*How to represent such wrappers?*

Information Extraction

Wrappers

AEFS

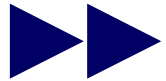
Learning



## *Elementary formal systems (EFS)*

$p(baX) :- p(aX) .$   
 $p(bbX) :- p(bX) .$   
 $p(abX) :- p(bX) .$   
 $p(a) .$   
 $p(b) .$   
 $p(ab) .$   
 $p(ba) .$   
 $p(bb) .$

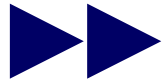
- $\Sigma = \{a,b\}$  ... characters
- $\Pi = \{p\}$  ... predicate symbols
- $X = \{X\}$  ... variables
- patterns like  $baX, aX, a$
- atoms like  $p(baX), p(aX), p(a)$
- rules like  $p(baX) :- p(aX) ., p(a) .$
  
- EFS  $S = (\Sigma, \Pi, \Gamma)$ , where  $\Gamma$  is a set of rules



## *EFS Semantics*

- relies on a well-known idea from logic programming; i.e., we focus our attention on ground atoms (g.a.)
  - for an EFS  $S = (\Sigma, \Pi, \Gamma)$ , we let
$$\text{Sem}(S) = \{ \text{g.a.} \mid \text{g.a. holds in all Herbrand models for } S \}$$
- characterizations of  $\text{Sem}(S)$ 
  - $\text{Sem}(S) = \{ \text{g.a.} \mid \text{g.a. holds in the least Herbrand model for } S \}$
  - thus, it suffices to enumerate the g.a. that hold in a distinguished model (using a simple operator, starting with the empty set)





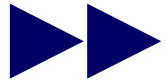
## *Advanced elementary formal systems (AEFS)*

```
q(X) :- not p(X) .  
p(XY) :- p(X) .  
p(YX) :- p(X) .  
p(aa) .
```

- characters, variables, patterns, atoms ... as for EFS
- rules as for EFS and, additionally, rules like  $q(X) :- \underline{\text{not}} p(X)$ .
- AEFS  $S = (\Sigma, \Pi, \Gamma)$ , where  $\Gamma$  is a set of rules that meet particular syntactical constraints

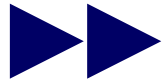
Why syntactical constraints at all?

if negation is allowed for, there is generally no least Herbrand model and, thus, the idea to enumerate the ground facts that hold in a distinguished model doesn't work



## *AEFS Semantics*

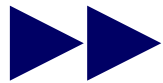
- similarly as before, for an AEFS  $S = (\Sigma, \Pi, \Gamma)$ , we let
$$\text{Sem}(S) = \{ \text{g.a.} \mid \text{g.a. holds in all Herbrand models for } S \}$$
- the introduced syntactical constraints on the rules in  $\Gamma$  guarantee that we obtain the same characterizations of  $\text{Sem}(S)$ , i.e.,
$$\text{Sem}(S) = \{ \text{g.a.} \mid \text{g.a. holds in the least Herbrand model} \}$$



*EFS/AEFS definable languages*

```
q(X) :- not p(X) .  
p(XY) :- p(X) .  
p(YX) :- p(X) .  
p(aa) .
```

- let an AEFS  $S = (\Sigma, \Pi, \Gamma)$  and some distinguished predicate symbol  $p$  from  $\Pi$  be fixed, then  
 $L(S, p) = \{ w \in \Sigma^+ \mid (w) \in \text{Sem}(S) \}$



## Variable-bounded EFS/AEFS

examples:

```
q(X) :- not p(X) .  
p(XY) :- p(X) .  
p(aa) .
```

- every variable in the body of a rule has to appear in the head, as well

counterexamples:

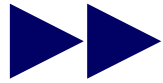
```
p(XY) :- p(X) , q(Y, Z) .
```

**Theorem:**

$L \in L(\text{vb-EFS})$  iff\*  $L$  is a r.e. language.

**Theorem:**

There are  $L \in L(\text{vb-AEFS})$  that are not r.e.



## *Length-bounded EFS/AES*

examples:

```
q(X) :- not p(X) .  
p(XY) :- p(X) .  
p(aa) .
```

- variable-bounded
- if some  $X$  appears  $k$  times in the body of a rule, it must occur at least  $k$  times in its head

counterexamples:

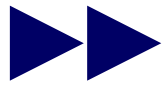
```
p(XY) :- p(X), q(Y, Y) .
```

**Theorem:**

$L \in \mathbf{L}(\mathbf{lb}\text{-EFS})$  iff\*  $L$  is context-sensitive.

**Theorem:**

$L \in \mathbf{L}(\mathbf{lb}\text{-AEFS})$  iff  $L$  is context-sensitive.



## *Regular EFS/AEFS*

examples:

```
q(X) :- not p(X) .  
p(XY) :- p(X) .  
p(aa) .
```

- length-bounded
- only unary predicate symbols
- only regular patterns in the head of a rule

counterexamples:

```
p(XYX) :- p(X) .  
p(XY) :- q(X, Y) .
```

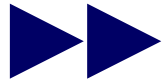
**Theorem:**

**$L \in L(\text{reg-EFS})$  iff  $L$  is context-free.**

**Theorem:**

**There are  $L \in L(\text{reg-AEFS})$  that are not context-free.**

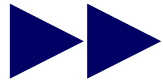
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*Closedness properties*

**Theorem:**

The AEFS definable language classes  
 $L(\text{reg-AEFS})$ ,  $L(\text{lb-AEFS})$ , and  $L(\text{vb-AEFS})$   
are closed under the operation union,  
intersection, and complement.



*Representing island wrappers as AEFS*

```
extract(V1, V2, X1L1V1R1X2L2V2R2X3) :-  
    l1(L1), r1(R1), l2(L2), r2(R2),  
    nc-r1(V1), nc-r2(V2), nc-l2(X2).
```

```
nc-r1(X) :- not c-r1(X).
```

```
c-r1(X) :- r1(X).
```

```
c-r1(XY) :- c-r1(X).
```

```
c-r1(XY) :- c-r1(Y).
```

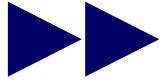
```
nc-r2(X) :- analogously
```

```
nc-l2(X) :- analogously
```

$l_1(X)$ ,  $r_1(X)$ ,  $l_2(X)$ ,  $r_2(X)$  *freely definable*



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*Learning*

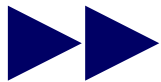
Information Extraction

Wrappers

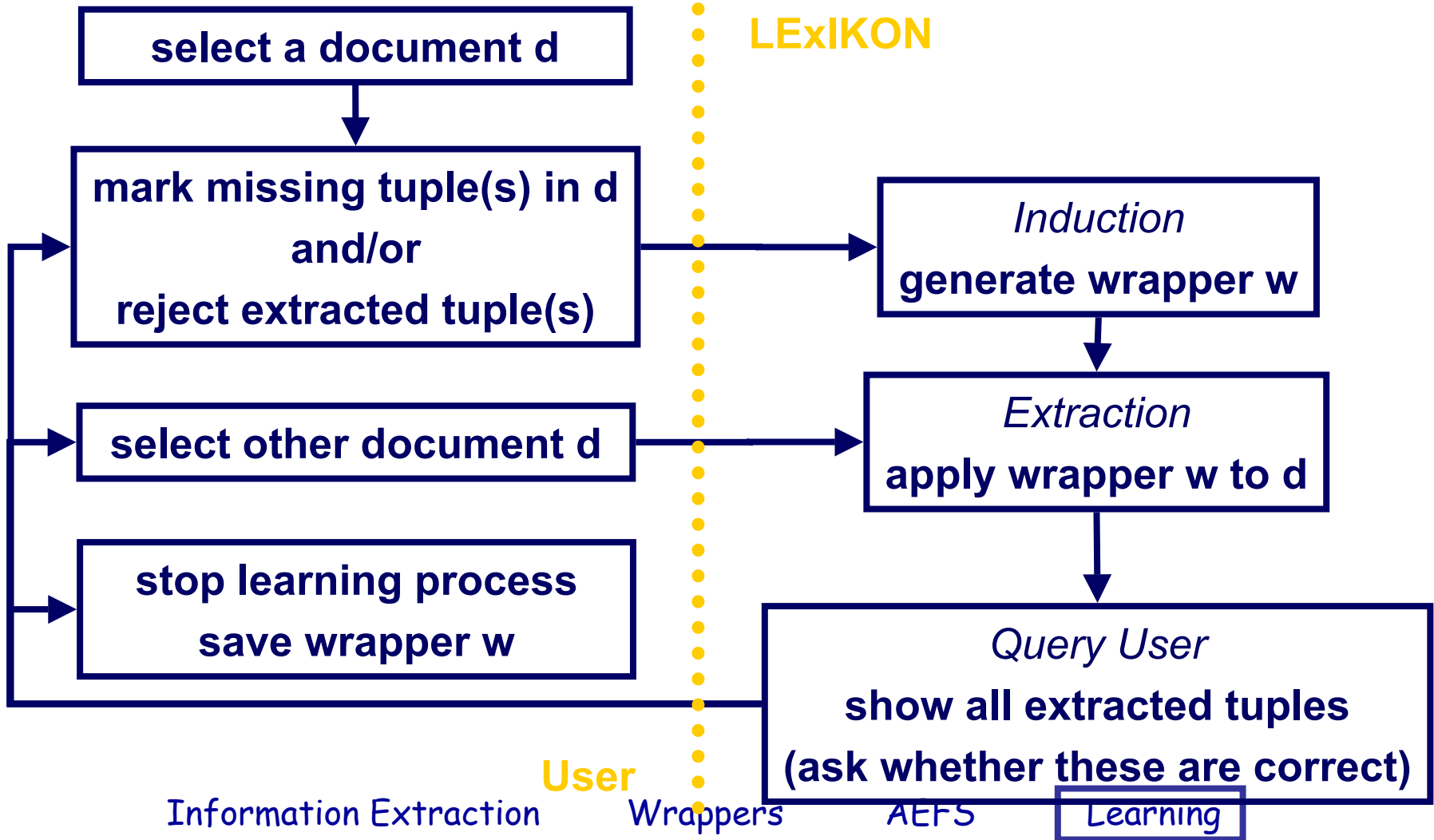
AEFS

Learning

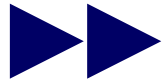
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*Interaction in LEXIKON*

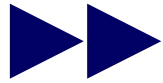


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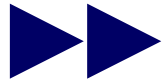
*Learning*

- **When is this interaction cycle successful?**  
→ **Learning**
- **2 different models**
  - learning in the limit
  - PAC learning
- **learnability results for**
  - representation language (AEFS)
  - island wrappers
  - composite learning tasks



*Learning in the limit*

- learning goal
  - a finite description of a target language  $L$
- information available about a target language  $L$ 
  - learning from positive data (text)  
sequence of words exhausting  $L$
  - learning from positive and negative data (informant)  
sequence of labelled words that exhausts  $\Sigma^+$ ; the words are labelled by '+' and '-' according to their membership in  $L$
- IIM
  - receives as input finite segments of a text (an informant) and outputs a hypothesis about the target language
  - learns  $L$  in the limit iff, on every text/informant, the sequence of hypotheses stabilizes on a correct description of the target language  $L$



## Results

**LimInf/LimTxt: set of all languages learnable from Informant/Text**

**Theorem:**

$$\mathbf{L(lb-EFS) \in LimInf}$$

**Theorem:**

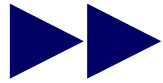
$$\mathbf{L(lb-AEFS) \in LimInf}$$

**Theorem:**

- (i)  $\mathbf{L(lb-EFS) \notin LimTxt}$
- (ii)  $\mathbf{L(lb-EFS(k)) \in LimTxt}$  for  $k \in \mathbf{N}$

**Theorem:**

- (i)  $\mathbf{L(lb-AEFS) \notin LimTxt}$
- (ii)  $\mathbf{L(lb-AEFS(1)) \in LimTxt}$
- (iii)  $\mathbf{L(lb-AEFS(k)) \notin LimTxt}$  for all  $k > 1$



*Learning island wrappers*

- remember:



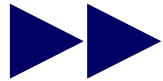
- available information / examples:



- task: learn delimiter languages  $L_1, R_1, \dots, L_n, R_n$   
from examples of form

$$\Sigma^* L_1 \{ \# \} \Sigma_{R_1} \{ \# \} R_1 \Sigma_{L_2} L_2 \dots L_n \{ \# \} \Sigma_{R_n} \{ \# \} R_n \Sigma^*$$

where  $\Sigma_L = \Sigma^* \setminus (\Sigma^* L \Sigma^*)$



## Results

**IW(L): set of all island wrappers with delimiter  
languages from L**

**Theorem:**

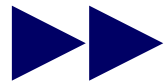
$$\mathbf{IW(\emptyset(\Sigma^*)) \in \text{LimInf}}$$

**Theorem:**

$$\mathbf{IW(\emptyset(\Sigma^*)) \notin \text{LimTxt}}$$

**Theorem:**

$$\mathbf{IW(\emptyset(\Sigma^k)) \in \text{LimTxt for } k \in \mathbb{N}}$$



*Subtasks when learning island wrappers*

- problem A: learn  $L_1$  from  $\Sigma^*L_1$
- problem B: learn  $R_n$  from  $\Sigma_{R_n}\{\#\}R_n\Sigma^*$
- problem C: learn  $R_m$  and  $L_{m+1}$  from  $\Sigma_{R_m}\{\#\}R_m\Sigma_{L_{m+1}}L_{m+1}$



A

C

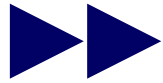
C

B

- problem D: learn delimiter languages from standard information (reference problem)



Information Extraction by Grammatical  
Inference  
G. Grieser



*Results*

**Theorem:**

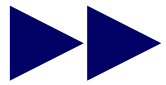
**The learning problems A, B, C, and D  
are incomparable.**

Information Extraction

Wrappers

AEFS

Learning



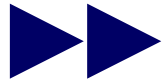
*example*

- $\Sigma = \{a, b, c\}$
- $L_0 = \{a^m b \mid m \geq 1\} \cup \{c\}$
- $L_{n+1} = \{a^m b \mid 1 \leq m \leq n+1\} \cup \{c, ca\}$

problem A (learn  $L$  from  $\Sigma^* L$ ) **solvable**

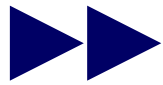
M: on input  $w_0, \dots, w_m$  check whether some string ends with  $a$ . If no such string occurs, output a description for  $\Sigma^* L_0$ , otherwise for  $\Sigma^* L_1$

problem B (learn  $R$  from  $\Sigma_R \{ \# \} R \Sigma^*$ ) **not solvable**



## *PAC learning*

- learning goal
  - finite description that approximates  $L$  sufficiently well
- learning algorithm
  - receives a finite set of positive and negative examples and computes a hypothesis about the target language  $L$
- $C$  is polynomial-time PAC-learnable iff there exists a learning algorithm  $A$  such that given  $\varepsilon, \delta \in [0, 1]$ ,  $n \in \mathbb{N}$ , and any probability distribution  $\text{Pr}$  over  $\Sigma^n$ 
  - $A$  takes  $q(1/\varepsilon, 1/\delta, n, s)$  examples randomly generated with respect to  $\text{Pr}$  and outputs, in polynomial time, a hypothesis  $h$  such that, with probability  $1 - \delta$ ,  $\text{Pr}(w \in L \Delta h) < \varepsilon$   
here,  $s$  denotes the size of the smallest description of  $L$



## Hereditary EFS/AEFS

examples:

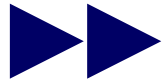
```
q(X) :- not p(X) .  
p(abXaY) :- p(bX), q(Y) .
```

- every pattern in the body of a rule is a subword of a pattern in its head

counterexamples:

```
p(aXbY) :- p(aaX) .
```

- $h\text{-}(A)\text{EFS}(m,k,t,r)$  - set of all hereditary (A)EFS with
  - at most  $m$  rules
  - at most  $k$  variables occurrences in head of every rule
  - at most  $t$  atoms in the body of every rule
  - arity of each predicate symbol at most  $r$



## Results

### Theorem:

For all  $m, k, t, r \in \mathbb{N}$ ,  $L(\text{h-EFS}(m, k, t, r))$  is polynomial time PAC learnable.

### Theorem:

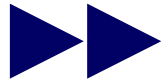
For all  $m, k, t, r \in \mathbb{N}$ ,  $L(\text{h-AEFS}(m, k, t, r))$  is polynomial time PAC learnable.

Note, that already  $L(\text{h-AEFS}(2, 1, 1, 1)) \setminus L(\text{h-EFS}) \neq \emptyset$ .

### Corollary:

If  $L$  is polynomial time PAC learnable then also  $IW(L)$  is polynomial time PAC learnable.

# Information Extraction by Grammatical Inference G. Grieser



## Overview

- Information extraction
- wrappers
  - island wrappers
- representation language
  - EFS, AEFS
  - representability
- learning
  - learning models LIM and PAC
  - learning of AEFS, of island wrappers, and of the subtasks

Information Extraction

Wrappers

AEFS

Learning